Determine if the series converges or diverges. Show the necessary information to justify your answer.

1.
$$\sum_{n=1}^{\infty} \frac{2n^2 + 3n + 1}{3n^2 + 2}$$
 2.
$$\sum_{n=0}^{\infty} 5 \left(\frac{5}{4}\right)^n$$
 3.
$$\sum_{n=0}^{\infty} 3 \left(\frac{1}{2}\right)^n$$

$$2. \qquad \sum_{n=0}^{\infty} 5 \left(\frac{5}{4}\right)^n$$

$$3. \qquad \sum_{n=0}^{\infty} 3 \left(\frac{1}{2}\right)^n$$

Find the interval of convergence of the geometric series, and, within this interval, the sum of the series as a function of x.

$$4. \qquad \sum_{n=0}^{\infty} \frac{\left(x-1\right)^n}{4^n}$$

Determine if the series converges or diverges. Show the necessary information to justify your answer.

$$5. \sum_{n=1}^{\infty} \frac{n}{n^2 + 1}$$

6.
$$\sum_{n=1}^{\infty} \frac{1}{2^n + 1}$$

7.
$$\sum_{n=1}^{\infty} \frac{3}{n+1}$$

8.
$$\sum_{n=1}^{\infty} \frac{2}{n^{4/3}}$$